

Discovering Subtypes of Neurodegenerative Progression with a Scalable Connectome-Constrained Dynamic Model

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Abstract. Parkinson's disease is clinically and biologically heterogeneous, yet its spatiotemporal progression remains poorly characterized. We present a connectome-constrained disease progression model that jointly estimates subject-specific disease time and data-driven subtypes from longitudinal morphometry. Applied to 85 imaging and clinical biomarkers from the Parkinson's Progressive Markers Initiative (PPMI) cohort, the model recovers four morphologically distinct progression subtypes. We validate the model on a hold-out cross-sectional dataset and benchmark it against SuStaIn under a matched training and validation protocol. Only our method recovers subtypes that correspond significantly to clinical motor subtypes and genetic variants of Parkinson's Disease.

Keywords: Disease progression modeling · Neurodegeneration · Subtype discovery · Connectome · Parkinson's disease · Cortical thickness

1 Introduction

Models of disease progression (DPM) offer a means to simulate treatment effect – sometimes called “digital twins” – and to estimate pre-symptomatic time of disease onset. Conventional DPM's in the context of neuroimaging infer long-term biomarker trajectories by “stitching together” longitudinal observations collected over a relatively short period from large sample sets. The problem requires simultaneous estimation of the canonical trajectory as well as each patient's disease score, typically treated as the free “time” variable mapping the patient to the trajectory. Established models include discrete-time [5, 15] and continuous-time variants [9, 14]. Several continuous-time DPMS use non-linear dynamics constrained by structural connectivity [10, 6, 1, 4, 11], providing a mechanistic framework that mirrors “prion-like” transsynaptic transmission of disease agents. A related challenge in progression modeling is disease heterogeneity. Patients with in the same general diagnostic category often follow distinct progression patterns,

motivating subtype discovery within DPMs. Subtyping progression models exist [15, 14], but are generally either not scalable to large numbers of biomarkers or lack the generative mechanistic power of network-based models. As highlighted in recent reviews [16, 8], a critical gap remains in our current modeling arsenal: the lack of approaches that simultaneously leverage the brain’s connectivity structure, scale to large numbers of brain regions, accommodate disease heterogeneity, and provide mechanistic interpretability over extended time ranges. In this work, we extend the recently proposed network-constrained COMIND model [11] to enable simultaneous modeling of nonlinear network dynamics and disease subtype identification. Our proposed method models neurodegeneration as a system of coupled logistic-diffusion trajectories constrained by structural connectivity, and performs automatic subtype discovery by inferring distinct spatial patterns of regional pathology sources from longitudinal imaging data.

2 Methods

A number of the proposed progression models have used logistic evolution as the basic model-building element. The idea is appealing as it mirrors our intuition that neurodegeneration has a gradual onset, a period of rapid advance, and a saturation point. Indeed, the sigmoid is a solution to the logistic ODE $\dot{x} = k(1 - x)x$, a dynamic in which the rate of accumulation is a product of self-supply and capacity. Our motivation is to incorporate network dynamics into this idea, while maintaining the asymptotic properties of the univariate logistic ODE, and to identify disease subtypes characterized by distinct patterns of regional pathology.

2.1 Dynamic Propagation Model

We begin by considering a dynamic p -dimensional system of accumulating neurodegenerative effects with a static transition matrix $K \in \mathbb{R}^{p \times p}$ defined in some way by brain connectivity. As in a standard logistic differential equation, we define the rate of neurodegenerative accumulation as a product of the present state of neurodegeneration and remaining capacity. This can be expressed as

$$\frac{d\mathbf{x}}{dt} = [I - D(\mathbf{x})]K\mathbf{x}, \quad \mathbf{x} \in [0, 1]^p \quad (1)$$

Here, $D(\mathbf{x})$ is the diagonal matrix with entries in $\mathbf{x}$. We consider external sources of neurodegeneration as constant, again contributing to the rate of regional accumulation in proportion to regional capacity.

$$\frac{d\mathbf{x}}{dt} = [I - D(\mathbf{x})][K\mathbf{x} + \mathbf{f}], \quad \mathbf{x} \in [0, 1]^p, \quad \mathbf{f} \in [0, \infty)^p, \quad (2)$$

where $\mathbf{f}$ represents the constant "forcing" term in the ODE. For the k^{th} individual regional biomarker, this is equivalent to

$$\dot{x}^k(t) = (1 - x^k) \left(\sum_m K_{km} x^m + f^k \right),$$

The transition matrix combines two parameters governing regional connectivity: network mediated propagation along the connectome, and local, connectivity-independent accumulation. Formally,

$$K = s_t K^* + \text{diag}(\boldsymbol{\kappa}), \quad (3)$$

where s_t is a scalar timescale governing the strength of network-mediated propagation and $\boldsymbol{\kappa} \in \mathbb{R}^p$ is a vector of region-specific self-propagation rates. Finally, to construct canonical trajectories of neurodegeneration we must scale solutions of the dynamic system to the natural scale of imaging biomarkers. This adds a scaling vector $\mathbf{s} \in \mathbb{R}^p$ to our trajectory parameter set. Suppose $\mathbf{x}(t)$ is the solution to (2). The predicted biomarker value at time t is then $\hat{\mathbf{y}}(t) = \mathbf{s} \odot \mathbf{x}(t)$, where $\odot$ is element-wise multiplication.

To account for population heterogeneity, we define Z subtypes. Each subtype $z \in \{1, \dots, Z\}$ has its own forcing term $\mathbf{f}_z$, representing a distinct spatial pattern of external pathology sources, while s_t and $\mathbf{s}$ are shared globally across subtypes. Each subject receives a hard assignment to the subtype whose predicted trajectory yields the lowest reconstruction error at their estimated disease time. The full parameter set is $\theta = \{s_t, \kappa, \mathbf{s}, \mathbf{f}_1, \dots, \mathbf{f}_Z\}$, with $2p + 1$ global parameters and $Z \cdot p$ subtype-specific forcing parameters.

2.2 Modeling Subject-Specific Time-Shift

As is common practice, we assume a Gaussian i.i.d. noise model. For the k^{th} biomarker y_{ij}^k measured in subject i at timepoint j , biomarker likelihood is expressed as

$$P(y_{ij}^k \mid \theta, \beta_i, z_i) = \mathcal{N}(y_{ij}^k \mid \hat{y}^k(t_{ij} + \beta_i; \theta_{z_i}), \sigma_k). \quad (4)$$

Here, β_i is the subject-specific "disease-time" or time-shift at the initial scan, and t_{ij} is the time of scan at visit j , given that $t_{i0} = 0$. To discourage subtypes from separating primarily along β_i rather than underlying progression pattern, we add a Jensen-Shannon divergence penalty weighted by λ_{jsd} that encourages distributions of time-shifts to be similar across subtypes.

2.3 Biomarker Trajectory Conditioning and Likelihood Estimation

To represent the fact that brain function is largely self-contained and locally protected from external inputs, we assume that the number of brain regions affected by $\mathbf{f}$ is small and therefore $\mathbf{f}$ is sparse. We place the same sparsity assumption on the self-connection term $\boldsymbol{\kappa}$, reflecting the expectation that local connectivity-independent accumulation is relevant in only a subset of regions. To prevent the timescale from collapsing to zero or diverging, we place a log-normal prior on s_t around a prior value s_{pr} . The complete prior on model parameter is

$$P(\theta) \propto \exp \left[-\lambda_f \sum_{z=1}^Z \|\mathbf{f}_z\|_1 - \lambda_\kappa \|\boldsymbol{\kappa}\|_1 - \frac{\lambda_s}{2} \left(\log \frac{s_t}{s_{\text{pr}}} \right)^2 - \lambda_s \|\mathbf{s}\|_2^2 \right] \quad (5)$$

Combining the terms in (4) and (5), we have the posterior for θ and β :

$$P(\theta, \beta, \mathbf{z} \mid \mathbf{y}) = \prod_{ijk} P(y_{ij}^k \mid \theta, \beta_i, z_i) \times P(\theta) \quad (6)$$

Subtype priors $P(z_i) = 1/Z$ are assumed uniform.

2.4 Model Estimation

We estimate model parameters and subject time-shifts using a generalized Expectation-Maximization approach. To reduce sensitivity to local optima, the algorithm is run from multiple random initializations of β and subtype assignments $\mathbf{z}$, retaining the solution with the lowest training loss. The number of subtypes Z is selected using the Bayesian Information Criterion (BIC), penalizing model complexity to avoid selecting an unnecessarily large number of subtypes. The effective parameter count ν includes the p entries of $\mathbf{s}$, the global timescale s_t , the number of nonzero entries of $\boldsymbol{\kappa}$, and the number of nonzero forcing term entries across all subtypes. The observation count n is the total number of scalar measurements, i.e. the sum over all subjects of visits times biomarkers. The log likelihood term is the sum of per-biomarker squared residuals normalized by the observed variance of each biomarker.

Algorithm 1 SubtypingEM

Require: observations $\mathbf{y}$, connectome K^* , number of subtypes Z

Ensure: $\theta = \{s_t, \boldsymbol{\kappa}, \mathbf{s}, \mathbf{f}_1, \dots, \mathbf{f}_Z\}$, β , $\mathbf{z}$

- 1: Initialize β , $\mathbf{z}$ randomly; initialize $\mathbf{f}_z$ for each subtype
 - 2: **while** not converged **do**
 - 3: Update $\mathbf{s}$, s_t , $\boldsymbol{\kappa}$ with β , $\mathbf{z}$, $\{\mathbf{f}_z\}$ fixed (L-BFGS)
 - 4: $z_i \leftarrow \arg \min_z \mathcal{L}_{\text{recon}}(\beta_i, \mathbf{y}_i; \theta_z)$ for each subject i
 - 5: Update each $\mathbf{f}_z$ using subjects with $z_i = z$ (L-BFGS)
 - 6: Update all β_i jointly via (6) with JSD regularization (L-BFGS)
 - 7: **end while**
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3 Data and Experiments

Synthetic Data generation We validated COMIND on synthetic data generated from three ground-truth subtypes, each governed by (2) with $p = 3$ biomarkers and a shared, fixed connectivity matrix K and shared scalar coupling $\alpha = 0.2$. Subtypes differ only in their forcing terms $\mathbf{f}$, with each subtype assigned a single nonzero forcing entry at a distinct biomarker index; this construction directly tests whether EM can recover subtype-specific forcing patterns from a shared network structure. For each subtype, 100 subjects were simulated with 3 observations each, sampled at yearly intervals along a 7-year disease-time axis, with

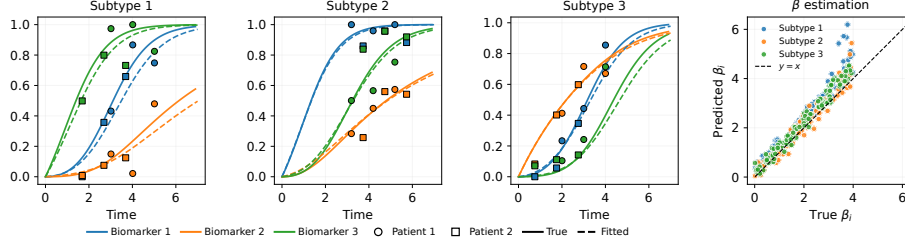


Fig. 1. Synthetic validation and trajectory recovery for three ground-truth subtypes. **Left three:** Trajectory recovery. Each column corresponds to one subtype. Noisy patient observations with fitted trajectories (dashed) against ground-truth (solid). **Right:** Synthetic validation. predicted vs. true subject time-shifts β . Points are centered on the $\hat{\beta} = \beta$ line, indicating unbiased recovery. The assigned subtype co-clustered with true subtype nearly perfectly (Adjusted Rand Index = 0.96).

Gaussian observation noise ($\sigma = 0.1$) added to all biomarkers. We additionally generated a privileged clinical feature per observation as $a(\beta_i + t_{ij} + \mathcal{N}(0, 1)) + b$, with slope $a \in [1, 5]$ and bias $b \in [0, 10]$, to test the model’s clinical-informed initialization pathway: subject time-shifts β are initialized via a linear mixed-effects model fit to these clinical scores, and forcing terms are initialized from the leading eigenvectors of K^* . Models were fit for $Z \in \{2, 3, 4\}$ with 3-fold cross-validated hyperparameter selection, and Z was chosen by BIC. Trajectory and sample generation for each subtype are shown in Fig. 1.

3.1 Parkinson’s Disease Imaging and Clinical Data

The PPMI study employs a standardized high-resolution 3D T1-weighted volumetric sequence (MP-RAGE/IR-FSPGR) acquired on 3T scanners across 50 international sites (sagittal $1.0 \times 1.0 \times 1.0$ mm isotropic scan, 256^3 FOV). We used 313 PPMI subjects with Parkinson’s Disease, yielding 622 total observations. T1-weighted scans were processed using FreeSurfer 7.0 to harmonize cortical and subcortical parcellations (Desikan-Killiany atlas, DK) across the time points, and residual site effects were removed using ComBat harmonization. We use cortical thickness measures 68 DK regions and 14 subcortical regions, expressed as deviation Z-scores relative to a normative reference cohort as our primary biomarker. The Z-scores were floored at ± 6 SD, sign-flipped so pathology corresponds to increasing biomarker value, and each biomarker was translated by its own minimum so all values are non-negative, as required by the model. Additional clinical measures included Montreal Cognitive Assessment (MoCA), Tremor-dominant sub-score (TD-Score) and Postural Instability-Gait Disorder Subscore (PIGD-score) from MDS-UPDRS-III symptom-specific items. Lower MoCA and higher TD/PIGD scores imply greater symptom severity.

3.2 Connectome Model

We used the precomputed structural connectivity matrix from the IIT Human Brain Atlas v5.0 [3], which was derived from whole-brain tractography on a HARDI template. Tractography was performed using Anatomically-Constrained Tractography (ACT) and filtered with the Spherical-deconvolution Informed Filtering of Tractograms (SIFT) algorithm. Streamlines were mapped onto the 82 cortical and subcortical regions of the Desikan-Killiany atlas to produce a group-level connectivity matrix. We retained only the top 10% of connections by streamline count, verified that no regions became disconnected after thresholding, and normalized the resulting matrix by its median row sum. Self-connections were set to zero. Zero padding was added to the connectome to accommodate clinical measures as disconnected regions in the model.

3.3 Parkinson’s Disease Experiments

We split subjects by number of visits: 126 patients with longitudinal follow-up (435 observations) formed the training set, and 187 with a single cross-sectional scan formed the hold-out validation set. We performed grid search over hyperparameters λ_f , λ_{scalar} , λ_{κ} , and λ_{jsd} , selecting the combination yielding the smallest BIC.

4 Results

4.1 Synthetic results

BIC correctly identified $Z = 3$ as the optimal number of subtypes over candidates $Z \in \{2, 3, 4\}$. Subtype-specific forcing terms were recovered accurately: in each case the dominant nonzero entry was correctly identified at the true biomarker index, with fitted values of 0.317, 0.302, and 0.249 against ground truth values of 0.3. The self-connection term κ was likewise recovered well: the true zero entry was correctly estimated as exactly zero by the sparsity prior, and the two nonzero entries (true 0.651, 0.604) were recovered as 0.726 and 0.650. Subtype classification achieved an Adjusted Rand Index of 0.96, and mean absolute time-shift error was 0.345 ± 0.317 years on a 7-year disease axis across 300 subjects. Subtype classification and time-shift recovery are shown in Fig. 1.

4.2 Parkinson’s Disease Model

BIC selected $Z = 4$ subtypes over candidates $Z \in \{2, 3, 4\}$. Subtype-specific trajectories for the regions showing the greatest pairwise ℓ_2 difference between subtype curves are shown in Fig. 3. Across the subtypes, different subsets of biomarkers drive progression, denoted by the magnitude of forcing terms across them. Subtype 1 is primarily driven by TD score, alongside pallidal and thalamic forcing terms. Subtype 2 is jointly driven by PIGD score and MCATOT, the two largest forcing terms in the model, together with strong bilateral putamen

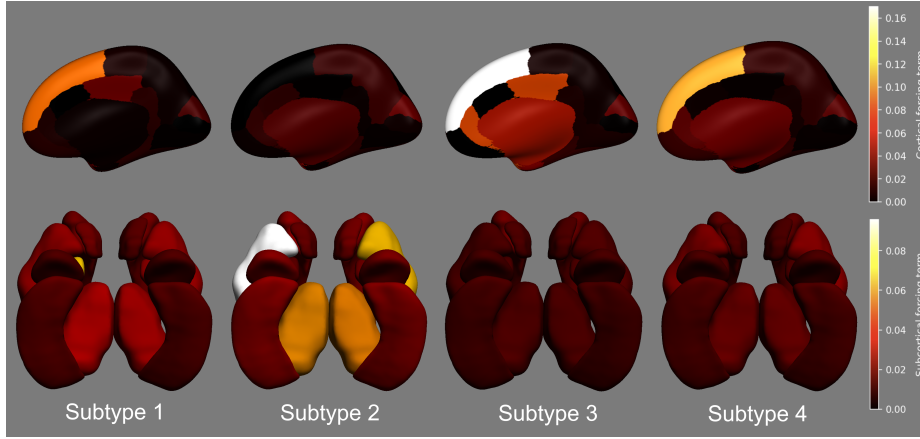


Fig. 2. Right-medial and axial view of brain region forcing terms

and thalamus forcing (Fig. 2). Subtype 3 is more cortically driven, primarily by entorhinal cortex, superior frontal cortex, and anterior cingulate. Subtype 4 is jointly driven by high TD and PIGD forcing, with greater forcing term in the superior frontal and temporal pole regions.

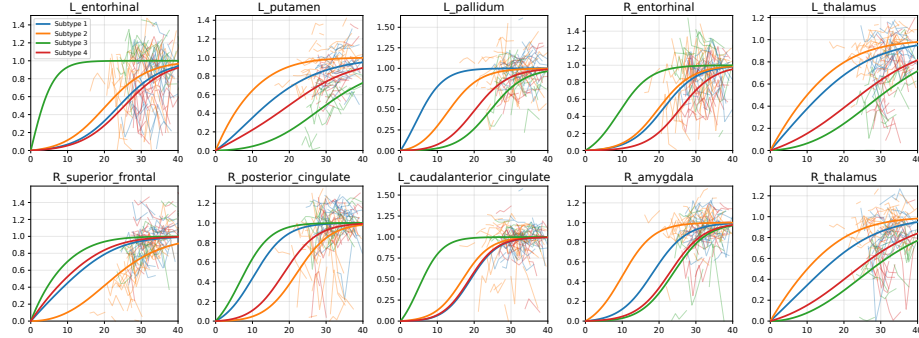


Fig. 3. Subtype-specific cortical thickness trajectories for the ten regions showing the greatest pairwise ℓ_2 difference between subtype curves. Observed subject trajectories are overlaid on each subtype's fitted curve.

4.3 Comparison to SuStaIn

To contextualize COMIND against a purely data-driven staging model, we fit SuStaIn [15] (pySuStaIn [2]) using the same underlying z-scored data, aggregated to 13 regions and 3 clinical scores for computational tractability, and the same

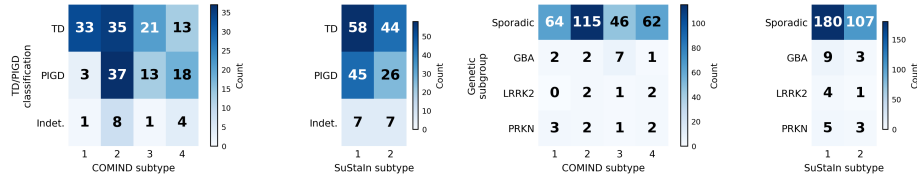


Fig. 4. Contingency tables of discovered subtype assignment versus clinical and genetic groupings. From left to right: COMIND and SuStaIn TD/PIGD/Indeterminate motor phenotype classification, held-out validation cohort ($n = 187$); COMIND and SuStaIn versus genetic subgroup (GBA, LRRK2, PRKN, sporadic PD), full cohort ($n = 312$).

training/validation split as COMIND; cross-validation favored a two-subtype solution, selected via pySuStaIn’s built-in cross-validation information criterion (CVIC), resembling the *Cortical* and *Subcortical* staging patterns reported by Shawa et al. [12] (Fig. 4). We compared subtype assignments from both methods against two independent groupings: TD/PIGD motor phenotype [13] and genetic subgroup (GBA, LRRK2, PRKN, sporadic PD), using χ^2 tests of independence (Fig. 4). On the hold-out validation cohort ($n = 187$), SuStaIn’s two subtypes showed no significant association with TD/PIGD classification ($\chi^2 = 1.22$, $df = 2$, $p = 0.543$), whereas COMIND’s four subtypes showed a significant association ($\chi^2 = 27.33$, $df = 6$, $p < 0.001$). The same pattern held for genetic subgroup across the full cohort ($n = 312$): SuStaIn showed no significant association ($\chi^2 = 1.35$, $df = 3$, $p = 0.717$), while COMIND showed a significant association ($\chi^2 = 17.80$, $df = 9$, $p = 0.038$). These results suggest COMIND’s connectome-constrained subtypes capture clinically and genetically meaningful structure.

5 Conclusion

We introduced a connectome-constrained progression model that jointly recovers subject-level disease time and morphologically distinct subtypes from cortical and subcortical trajectories. COMIND identified four progression subtypes in the PPMI cohort. These subtypes correspond significantly to genetic variants of PD prescribed by the GBA, LRRK2 and PRKN variants as well as clinical motor subtypes in a holdout dataset. A matched comparison to SuStaIn showed that both models recover a consistent subcortical-versus-cortical organizing structure despite their differing formulations. Validation on independent cohorts such as ENIGMA-PD [7] and incorporation of dynamically evolving connectome structure remain directions for future work.

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