

### Appendix I. Proof of the low-rank property between frames

Let  $\mathbf{u}_{r,t}$  represents the dynamic image of the  $r$ -th coil at the  $t$ -th time frame,  $\mathbf{u}_t$  is the coil-combined data. According to [9, 10], there exists  $\mathbf{w}_t$  such that  $\mathbf{u}_t \cdot \mathbf{w}_t = 0$ , meaning  $\mathbf{u}_1 \cdot \mathbf{w}_1 + \mathbf{u}_2 \cdot \mathbf{w}_2 + \dots + \mathbf{u}_n \cdot \mathbf{w}_n = 0$ . In a general scenario, for  $t_i$  and  $t_j$ , we have:

$$\begin{aligned} & \mathbf{u}_{i,t_i} \cdot \mathbf{S}_j \cdot \mathbf{w}_{t_i} + \mathbf{u}_{j,t_j} \cdot \mathbf{S}_i \cdot \mathbf{w}_{t_j} \\ &= \mathbf{S}_j \cdot \mathbf{S}_i (\mathbf{u}_{t_i} \cdot \mathbf{w}_{t_i} + \mathbf{u}_{t_j} \cdot \mathbf{w}_{t_j}) \\ &= \mathbf{S}_j \cdot \mathbf{S}_i \cdot 0 \\ &= 0 \end{aligned}$$

So,

$$\begin{aligned} \hat{\mathbf{u}}_{i,t_i} \cdot \hat{\mathbf{S}}_j \cdot \mathbf{w}_{t_i} + \hat{\mathbf{u}}_{j,t_j} \cdot \hat{\mathbf{S}}_i \cdot \mathbf{w}_{t_j} &= 0 \\ H(\hat{\mathbf{u}}_{i,t_i}, \hat{\mathbf{u}}_{j,t_j}) \begin{bmatrix} \hat{\mathbf{S}}_j \cdot \mathbf{w}_{t_i} \\ \hat{\mathbf{S}}_i \cdot \mathbf{w}_{t_j} \end{bmatrix} &= 0 \end{aligned}$$

### Appendix II. Derivation of Perturbation Kernel

Based on Eqs. 5 and the SDE theory in [22], the perturbation kernel of the proposed SDE can be expressed as:

$$p_{0t}(\mathbf{x}(t) | \mathbf{x}(0)) = \mathcal{N}(\mathbf{x}(t); e^{\frac{1}{2} \int_0^t \eta(s) \Phi ds} \mathbf{x}(0), \frac{1}{2} \int_0^t \beta(\tau) (e^{\int_\tau^t \eta(s) ds} d\tau e^{\Phi} \Omega_\Phi (e^{\Phi} \Omega_\Phi)^*), \quad t \in (0, 1])$$

By applying the Taylor expansion, the mean value  $\mu$  is determined as:

$$\begin{aligned} \mu &= e^{\frac{1}{2} \int_0^t \eta(s) \Phi ds} \mathbf{x}(0) \\ &= \left( \mathbf{I} + \frac{1}{2} \int_0^t \eta(s) \Phi ds + \frac{1}{2!} \left( \frac{1}{2} \int_0^t \eta(s) \Phi ds \right)^2 + \frac{1}{3!} \left( \frac{1}{2} \int_0^t \eta(s) \Phi ds \right)^3 + \dots \right) \mathbf{x}(0) \\ &= \mathbf{x}(0). \end{aligned}$$

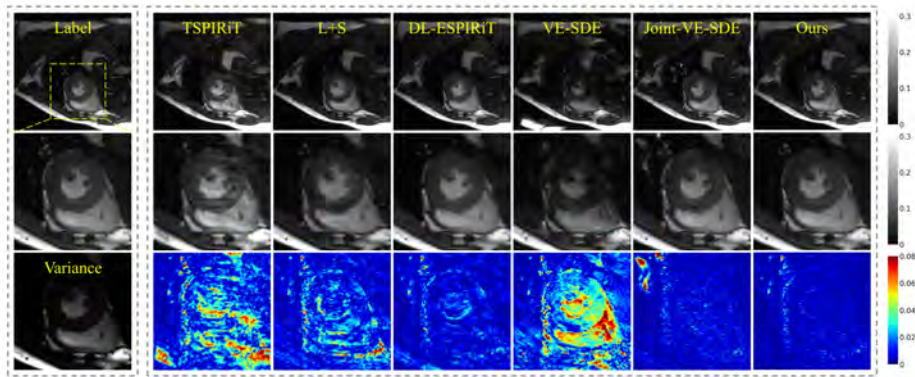
we denote  $\sigma = \sqrt{\frac{1}{2} \int_0^t \beta(\tau) e^{\int_\tau^t \eta(s) ds} d\tau}$ , the standard deviation of the perturbation kernel is expressed as:

$$\Sigma^{\frac{1}{2}} = \sigma \cdot e^{\Phi} \Omega_\Phi(\mathbf{I}) = \sigma \cdot \left( \mathbf{I} + \Phi + \frac{1}{2!} \Phi^2 + \frac{1}{3!} \Phi^3 + \dots \right) \Omega_\Phi(\mathbf{I}) = \sigma \cdot \Omega_\Phi(\mathbf{I})$$

So,

$$p_{0t}(\mathbf{x}(t) | \mathbf{x}(0)) = \mathcal{N}(\mathbf{x}(t); \mathbf{x}(0), \sigma^2 \Omega_\Phi \Omega_\Phi^*(\mathbf{I})), \quad t \in (0, 1])$$

## Appendix III. Visual results of systole image

Fig. 1. Visualization of systole image at  $R = 12$ .