## Supplementary material: LIBR+: Improving Intraoperative Liver Registration by Learning the **Residual of Biomechanics-Based Deformable** Registration

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(a) preoperative mesh of (b) LIBR-deformed mesh of (c) GT deformed mesh of liver model 1 without before liver model 1-L without be- liver model 1-L after left left forces applied.

fore left forces applied.

forces applied.

Fig. 1: Similar topology of preoperative (a), LIBR (b) and GT (c) deformed mesh after data coarsening. This gives a verified support of the assumption that a shared tetrahedron topology could be extracted from these three meshes after data coarsening.



(b) Surface Down-Sampling (c) Surface Reconstruction

Fig. 2: Pipeline of data coarsening process: (a) Surface Down-Sample, (b) Surface Down-Sampling, and (c) Surface Reconstruction. We take preoperative mesh of liver model 1 as an example.

| Data Splits             | Edge TRE |        |        |        | Inner TRE |        |     |        |
|-------------------------|----------|--------|--------|--------|-----------|--------|-----|--------|
|                         | wICP     | LIBR   | V2S    | SR-GCN | wICP      | LIBR   | V2S | SR-GCN |
| Surface data only       | 14.066   | 11.666 | 11.640 | 4.405  | 11.869    | 10.412 | /   | 4.412  |
| Surface + 1 US Plane    | 14.066   | 9.660  | 11.248 | 4.389  | 11.869    | 8.758  | /   | 4.402  |
| Surface $+ 2$ US Planes | 14.066   | 8.174  | 11.15  | 4.326  | 11.869    | 7.487  | /   | 4.338  |
| Surface $+ 3$ US Planes | 14.066   | 7.225  | 11.05  | 4.324  | 11.869    | 6.674  | /   | 4.345  |
| Surface + 16 US Planes  | 14.066   | 4.851  | 10.994 | 3.292  | 11.869    | 4.570  | /   | 3.341  |
| All Data                | 14.066   | 7.441  | 11.072 | 3.289  | 11.869    | 6.859  | /   | 3.322  |

Table 1: TRE separated by the category of intraopeartive measurements used.



Fig. 3: Ablative Component Comparison on different data splits: (B1) preoperative mesh as model's input. (B2) Concatenated preoperative and LIBR-deformed mesh as model's input. (B3) Bipartite Branch Integration on top of (B2). (B4) Sparse loss supervision on top of (B2). (Ours) All components.